

1. Solve the following 1st order DE

(a) $2x \frac{dy}{dx} + 3y = 4$ (16 scores)

(b) $\cos x - y \sin x + (1 + \cos x) \frac{dy}{dx} = 0$ (17 scores)

(c) $t^2 \frac{dy}{dx} + y^2 = ty$ (17 scores)

2. Solve the following higher order DEs

(a) $(1 - 2x - x^2)y''(x) + 2(1 + x)y'(x) - 2y(x) = 0$ (16 scores)

(Hint: $y = x + 1$ is one of the solutions)

(b) $y^{(4)}(x) + 2y^{(3)}(x) + y''(x) - 2y'(x) - 2y(x) = 1 + e^x$ (17 scores)

(c) $xy''(x) - y'(x) = \ln(x^2)$ (17 scores)